## KARNATAKA STATE WOMEN'S UNIVERSITY, BIJAPUR DEPARTMENT OF MATHEMATICS

The syllabus of Semester system in Mathematics for B.A. / B.Sc. Degree Course

1. The following table shows the details of number of teaching hours, number of Hours for problem solving, pattern of examination and allotment of marks for each semester.

| B.A./ B.Sc Degree Course | Standards | Semesters <br> I, II, III \& IV | Semester <br> V \& VI |
| :--- | :--- | :---: | :---: |
| Number of papers in Each <br> Semester |  | 2 | 3 |
| Teaching Hours Per Paper Per <br> Week | a) Teaching | 4 Hours | 4 Hours |
| b) Problem solving |  |  |  |
| Total (a+b) | 1 Hour <br> 5 Hours | 5 Hours |  |
| Examination pattern in each <br> paper in each semester | Duration of Examination | 3 Hours | 3 Hours |
| i) Examination marks | a) Maximum | 60 | 80 |
| ii) Internal Assessment |  |  |  |
| marks | b) Minimum for pass | 24 | 32 |
| iii) Total Marks | b) Minimum for pass | 15 | 20 |

2. Internal assessment marks in each paper shall be awarded by the concerned course teacher based on the two class tests each of one-hour duration conducted during the semester.
3. The internal assessment marks awarded shall be carried on for the repeated examinations.
4. The maximum strength of each semester for each section be restricted to SIXTY students.
5. Problem solving classes be conducted in batches of not more than $\mathbf{2 0}$ students in each batch.

## B.Sc. DEGREE

COURSE STRUCTURE FOR MATHEMATICS SUBJECT
[Duration 6 Semesters (3 Years)]

## SEMESTER-I

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 1.1 | Algebra-I | Mathematical Logic <br> Elements of Set Theory <br> Matrices |
| 1.2 | Calculus-I | Limits \& Continuity <br> Successive Differentiation <br> Polar Coordinates <br> Theory of Plane Curves |

## SEMESTER-II

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 2.1 | Algebra-II | Theory of Equations <br> Sequences <br> Infinite Series |
| 2.2 | Calculus-II | Integral Calculus <br> Application of Integral Calculus <br> Functions of Two \& Three Variables |

SEMESTER-III

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 3.1 | Vector Algebra and <br> Analytical Solid <br> Geometry | Vector Algebra and Analytical Solid Geometry |
| 3.2 | Real Analysis | Differentiability <br> Reimann Integration <br> Line \& Multiple Integration |

SEMESTER-IV

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 4.1 | Algebra-III | Abstract Algebra \& Linear Algebra |
| 4.2 | Differential Equations-I | Ordinary Differential Equations |

## SEMESTER-V

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 5.1 |  <br> Laplace Transform | Vector Analysis, Fourier Series and Laplace <br> Transforms |
| 5.2 | Differential Equations-II | Series Solution <br> Partial Differential Equations |
| 5.3 | Optional-I |  |

## SEMESTER-VI

| Paper No. | Paper Title | Content of Topics |
| :---: | :--- | :--- |
| 6.1 | Numerical Analysis | Numerical Analysis |
| 6.2 | Complex Analysis | Complex Analysis and Improper Integrals |
| 6.3 | Optional-II |  |

Students have to select ONE of the optional papers listed below during V Semester and corresponding paper during VI Semester (depending upon the teaching staff available and infrastructure available in the college).

## Optionals for Fifth Semester:

- 5.3(a) Mechanics-I
- 5.3(b) Graph Theory-I


## Optionals for Sixth Semester:

- 6.3(a) Mechanics-II
- 6.3(b) Graph Theory-II


## Mathematical Logic:

Revision of symbolic logic of simple and compound propositions, tautology, contradiction, valid arguments, the structure of mathematical systems. Direct and indirect proofs. Disproof by a counter example. Quantifiers, universal quantifiers, existential quantifiers and negation containing quantifiers.

## Elements of Set Theory:

Existence of inverse of a function and properties of inverse functions. Composition of functions. Associativity of inverse of composition. Countable and uncountable sets.

## Matrices:

Recapitulation of matrix algebra, rank of matrix, elementary operations, equivalent matrices, invariance of rank under elementary operation, inverse of a non-singular matrix by elementary operations.

System of m-linear equations in n unknowns, matrices associated with linear equation, criterion for existence of non-trivial solution of homogeneous and nonhomogeneous system, criterion for uniqueness of solutions.

Eigen values and eigen vectors of a square matrix upto third order standard properties, Cayley-Hamilton theorem - Applications.

## References:

1. F.J. Noronha, et al: Introduction to Mathematical Logic, (Bangalore University Publication).
2. F.Ayres: Matrices (Schaum Publishing Co.)
3. Y.F. Line and S.Y. Lio: Set Theory, Intuitive Approach (Houghton Mifflin Co.)
4. S.Lipschutz: Set Theory \& Related Topics (Schaum Publishing Co.)
5. Rudraiah et al: College Mathematics, Vol. I, (Sapna, Bangalore).
6. G.K.Ranganath: College Mathematics, Vol. I (Part-I), S.Chand \& Co. Ltd.

## Limits \& Continuity:

Recapitulations, algebra of continuous functions. Properties of continuous functions, differentiability, Rules of differentiation.

## Successive Differentiation:

$\mathrm{n}^{\text {th }}$ derivative of the functions $(a x+b)^{m}, \log (a x+b), e^{a x}, \sin (a x+b), \cos (a x+b)$, $e^{a x} \sin (b x+c), e^{a x} \cos (b x+c)$, Leibnitz theorem and applications. 06 Hrs

## Polar Coordinates:

Angle between the radius vector and the tangent. Angle of intersection of curves (polar form). Perpendicular from pole on to the tangent. Pedal equations. Derivative of an arc in Cartesian \& parametric and polar forms

## Theory of Plane Curves:

Points of inflection, concavity and convexity of curves. Curvature of plane curves. Formula for radius of curvature in Cartesian, parametric, polar and pedal form. Centre of curvature, evolutes and involutes. Envelopes, asymptotes, singular points, cusp, node and conjugate points. Tracing of standard curves in Cartesian, parametric and polar forms (cissoid, strophoid, Astroid, Folium of Descaries, Cycloid \& Cardiod).

## References:

1. Shanthi Narayan: Differential Calculus (S.Chand \& Co.).
2. Murray R. Spiegel: Advanced Calculus (Schaum Series).
3. L.Bers: Calculus, Vol. I \& II (IBM).
4. Rudraiah et al, College Mathematics, Vol. I, (Sapna, Bangalore)
5. F.Ayres Jr: Calculus, Schaum Series.
6. G.K.Ranganath: College Mathematics, Vol. I (Part-II), S. Chand \& Co. Ltd.

## PAPER 2.1: ALGEBRA-II

## Theory of Equations:

Relation between the roots and coefficients of general polynomial equation in one variable. Transformations of equations. Descartes' rule of signs. Solutions of equations for multiple roots (Cardons method).

## Sequences:

Sequences, sub-sequences, bounded and unbounded sequences. Convergence and divergence of sequences and subsequences, monotonic sequences, algebra of convergent sequences, limit superior and limit inferior of sequences, limit points as limit of convergent, subsequences. Cauchy sequences, Cauchy's criterion for convergence.

## Infinite Series:

Oscillation of series, properties of convergent series, properties of series of positive terms, geometric series, harmonic series. Test for convergence of series: p-series, comparison test, Cauchy's root test, D'Alemberts' ratio test, Raabe's test, absolute and conditional convergence, D'Alembert's test for absolute convergence - Alternating series, Leibnitz's test.

## References:

1. Uspenskey: Theory of Equations.
2. C.C.Macduffee: Theory of Equations (John Wiley).
3. Ray \& Sharma: Higher Algebra (S.Chand \& Co.)
4. Burnside and Porton: Theory of Equations (S.Chand \& Co.)
5. S.C.Malik: Mathematical Analysis (Wiley-Eastern).
6. Earl D.Rainville: Infinite Series, McMillan Co.
7. OE Stanaitis: An Introduction to Sequences, Series and Improper Integrals, Holdan-Dey Inc.
8. G.K.Ranganath: College Mathematics, Vol. I, S. Chand \& Co. Ltd.

## PAPER 2.2: CALCULUS-II

## Integral Calculus:

Recapitulation of definition of integration. Integrals of algebraic, trigonometric, rational and irrational functions. Definite integrals. Definite integral as limit of sum with examples. Standard reduction formulae
$\left(\int \sin ^{m} x d x, \int \cos ^{m} x d x, \int \tan ^{m} x d x, \int \cot ^{m} x d x, \int \operatorname{Sec}^{m} x d x, \int \operatorname{cosec}^{m} x d x\right.$, $\int \sin ^{m} \cos ^{n} x d x$ ) with examples

## Applications of Integral Calculus:

Computation of areas, surface areas and volumes of solids of revolution. Lengths of arcs for standard curves in Cartesian and polar forms.

## Functions of Two and Three Variables:

Continuity, partial derivatives, Euler's theorem for homogeneous functions (2variables). Maxima and minima of functions of two variables. Total derivative. Total differential, differentiation of implicit functions. Change of variables. Dependent and independent functions. Jacobian's properties and functional relations.

## References:

1. Shanthi Narayan: Integral Calculus (S.Chand \& Co.).
2. Murray R. Spiegel: Advanced Calculus (Schaum Series).
3. L.Bers: Calculus, Vol. I \& II (IBM).
4. Shanti Narayan: Differential Calculus (S.Chand \& Co.).
5. Rudraiah et al: College Mathematics, (Sapna, Bangalore).
6. G.K.Ranganath: College Mathematics, Vol. I, S. Chand \& Co. Ltd.

## Vector Algebra:

Recapitulation of vector algebra. Vector triple product. Product of four vectors. Reciprocal vectors.

## Analytical Solid Geometry:

Cartesian coordinates in three-dimensional space. Relation between Cartesian coordinates and position vectors. Distance and division formulae (in vector and Cartesian form). Direction cosines of a line (as components of a unit vector). Direction ratios of the join of two points. Projection on a straight line (vector and Cartesian form), angle between two lines (dot product and Cartesian forms). Area of a triangle and volume of a tetrahedron with given vertices (vector and Cartesian forms).

Equation of a plane in the form: (i) $(\vec{r}-\vec{a}) \hat{n}=0$ (ii) $\vec{r}=\vec{c}+l \vec{a}+m \vec{b}$
(iii) $|\vec{r}-\vec{a} \vec{b}-\vec{a} \vec{c}-\vec{a}|=0$ and their Cartesian equivalence. Plane through three points. Angle between planes. Equation of plane in the form (i) $\vec{r}=\vec{a}+\vec{b}$; (ii) $\vec{r}=[1-t] \vec{a}+t \vec{b}$ and their equivalent Cartesian forms. Angle between line and plane (vector and Cartesian forms). Condition for a line to lie in a plane (vector and Cartesian forms). Planes coaxial with given planes. Equation of the line of intersection of two planes. Perpendicular distance of a point from a line and plane. Planes bisecting the angle between two given planes co-planarity of two lines. Shortest distance between two lines (all these results are to be obtained in both vector and Cartesian forms).

## References:

1. S.L.Loney: Coordinate Geometry, Part-I (MacMillan)
2. Shanti Narayan: Elements of Analytical Solid Geometry (S.Chand \& Co.)
3. Khanna M.L.: Analytical Solid Geometry.
4. Bill R.J.T.: Coordinate Geometry of 3-Dimensions, McMillan India.
5. Spiegel M.R.: Vector Analysis (Schaum Series).
6. Shanti Narayan: Vector Algebra and Linear Algebra (S.Chand \& Co.)
7. G.K.Ranganath: College Mathematics, Vol. II, S. Chand \& Co. Ltd.

## Differentiability:

Rolle's theorem, Lagrange's and Cauchy's mean value theorem. Taylor's theorem with Lagrange's form of the remainder. Taylor's and Maclaurin's series. Problems on transcendental functions. Indeterminate forms, L'Hospital rules.

## Reimann Integration:

Recapitulation of real number system, postulates and their consequences, inequalities and absolute values, lower and upper bounds.

The upper and lower sums, necessary and sufficient conditions for integrability. Algebra of integrable functions. Intergrability of continuous and monotonic functions. Fundamental theorem of calculus, change of variables. Integration by parts. The first and second mean value theorems of integral calculus.

## Line and Multiple Integrals:

Definitions of a line integral, basic properties. Examples on evaluation of line integrals. Examples on differentiation under integral sign and integration under differential sign.

Definitions of double integral: its conversion to iterated integrals. Evaluation of double integrals (i) under given limits (ii) in regions bounded by given curve change of variables. Surface areas as double integrals.

Definition of a triple integral and evaluation. Change of variables. Volume as a triple integrals.

## References:

1. Shanti Narayan: Differential Calculus (S.Chand \& Co.)
2. Murray R. Spiegel: Advanced Calculus (Schaum's Series).
3. Sokoilnikoff I.S.: Advanced Calculus (McGraw Hill).
4. S.C.Malik: Mathematical Analysis (Wiley-Eastern)
5. Sharma and Vasistha: Real Analysis (Krishna Prakashan Mandir, Meerut).
6. G.K.Ranganath: College Mathematics, Vol. II, S. Chand \& Co. Ltd.

## PAPER 4.1: ALGEBRA-III

## Abstract Algebra:

Cyclic groups, cosets, Lagrange's, Fermat's and Eular's thermos. Normal sub-groups, Homorphism, Kernel of Homorphism, fundamental theorem of Homomorphism, Isomorphism. Permutation groups, rings, sub-rings, Integral domains, fields and their simple properties with examples.

## Linear Algebra:

Vector space examples Including $R^{n}$ and $C^{n}$. Properties of vector space: Subspaces. Criteria for a subset to be a subspace. Linear combination concepts of linearly independent and dependent subsets. Basis and dimension of a vector space and standard results related to a basis. Examples illustrating concept and results (with emphasis on $\mathrm{R}^{3}$ ). Linear transformations: Properties of linear transformations, matrix of a linear transformation, change of basis, range and Kernel of a linear transformation, rank nullity theorem.

## References:

1. Herstein I.N.: Topics in Algebra (Vikas)
2. Fraleigh J.B.: A first course in Abstract Algebra (Addison - Wesley).
3. Lipschitz S.: Linear Algebra (Schaum Series).
4. Shepherd G.C.: Vector space of Finite Dimension (Oliver and Boyed).
5. N.Jacobson: Basic Algebra, Vol. I \& II, Hindustan Pub. Co.
6. G.K.Ranganath: College Mathematics, Vol. II, S. Chand \& Co. Ltd.

## PAPER 4.2: DIFFERENTIAL EQUATIONS-I

Formation of differential equations, equations of first order and first degree (Homogeneous, Non- Homogeneous, exact, Non -Exact, Linear, Non- Linear) equations of first order and higher degree equations, solvable for $\mathrm{p}, \mathrm{x}, \mathrm{y}$. Clairaut's equations. Singular solutions. Linear equation with $\mathrm{n}^{\text {th }}$ order and constant coefficients. Particular integral when RHS is of the form $e^{a x}, x^{n} \sin a x$, $\cos a x, e^{a x} V, x V$ where $V$ is a function of $x$. Cauchy Euler differential equations of order two. Simultaneous differential equations (two variables) with constant coefficients. Solution of ordinary second order linear differential equations by the following methods:

1. When a part of complementary function is given
2. Changing the independent variable
3. Changing the dependent variable.
4. When a first integral is given (exact equation).
5. Variation of parameters

## References:

1. Daniel Murray: Introductory Course in Differential Equations (Orient Longman).
2. Chorlton F: Ordinary Differential \& Difference Equations (Van Norstrand).
3. Ayres F: Differential Equations (Schaum's Series).
4. Simmons G.F.: Differential Equations (T.M.H.)
5. Pisggio H.T.H.: Differential Equations (Orient Longmans)
6. Willim E. Boyce and Richard C.Diprima: Elementary Differential Equations and BVP (John Wiley \& Sons).
7. Rudraiah et al: College Mathematics, Vol. I \& II, (Sapna, Bangalore).
8. G.K.Ranganath: College Mathematics, Vol. II, S. Chand \& Co. Ltd.

## PAPER 5.1: VECTOR ANALYSIS AND LAPLACE TRANSFORMS

## Vector Analysis:

Scalar field, gradient of a scalar field, geometrical meaning, directional derivatives. Vector field, divergence and curl of a vector field. Solenoidal and irrotational fields. Laplacian of a scalar field. Vector identities. Expressions for $\nabla \phi$, div $\vec{f}$ and curl $\vec{f}$ in orthogonal, curvilinear coordinates and specialization to Cartesian, cylindrical and spherical coordinates. Greens, Gauss and Stokes theorems (Statements only) simple examples.

## Fourier Series:

Periodic functions. Fourier series of functions with period $2 \pi$ and period 2L. Half range cosine and sine series.

## Laplace Transform:

Definition and basic properties. Laplace transform of some common functions. Laplace transforms of the derivatives and the integral of a function. Laplace transform of the Heaviside and Dirac delta function - Convolution theorem. Inverse Laplace transforms: Application to ordinary linear differential equation of first and second order with constant coefficients.

## References:

1. Murray R, Spiegel L: Vector Analysis (Schaum Series).
2. Spain B: Vector Analysis (ELBS)
3. Murray R, Spiegel L: Laplace Transforms (Schaum Series).
4. Spain B and Smith M.G.: Functions of Mathematical Physics (Van-Norstrand).
5. Churchill RV and Brown JW: Fourier Series \& Boundary Value Problems (McGraw Hill).
6. G.K.Ranganath: College Mathematics, Vol. III, S. Chand \& Co. Ltd.

## PAPER 5.2: DIFFERENTIAL EQUATIONS-II

## Series Solution:

Legendre differential equation. Legendre polynomails $P_{n}(x)$ as a solution, Rodrigue's formula, generating polynomials theorem, orthogonal property and basic recurrence relations. Bessel differential equation. Bessel function $\mathrm{J}_{\mathrm{n}}(\mathrm{x})$ as a solution - generation formula - integral formula for $\mathrm{J}_{n}(\mathrm{x})$ : orthogonal property. Basic recurrence relations - problems there on.

## Total Differential Equation:

Necessary condition for the equation Pdx+Qdy+Rdz=0 to integral - problems there on. Solution of equation of the form $\frac{d x}{P}=\frac{d y}{Q}=\frac{d z}{R}$.

## Partial Differential Equations:

Formation of partial differential equations, Lagrange's linear equations $P p+Q q=R$. Standard types of first order linear partial differential equations and equations reducible to standard form. Charpit's method.

## References:

1. Boyce and Diprima Elementary Differential Equations and BVP (John Wiley \& Sons).
2. Simmons G.F.: Differential Equations (TMH).
3. Cholton F.: Ordinary Differential Equations (Von-Norstand).
4. Ayres F.: Differential Equations (Schaum Series)
5. Ian N.Sneddan: Elements of Partial Differential Equations, McGraw Hill.
6. Stephenson G: An introduction to Partial Differential Equations (ELBS).
7. G.K.Ranganath: College Mathematics, Vol. III, S. Chand \& Co. Ltd.

## PAPER 6.1: NUMERICAL ANALYSIS

Errors: Classification of errors (absolute, rounding, relative and percentage errors). Relations connecting the errors with illustrations.

Solution of non-linear equations: method of successive bisection, method of false position, Newton-Raphson's iterative method, the secant method.

Solution of system of equations: Gauss elimination method, Jacobi method, Gauss-Seidel method.

Finite Differences: Definition and properties of $\Delta, \nabla$ and $E$ and relations between them. The $\mathrm{n}^{\text {th }}$ differences of a polynomial.

Interpolation: Newton-Gregory forward and backward interpolation formulae, Lagrange's and Newton's interpolation formula for unequal intervals, inverse interpolation.

Numerical differentiation using forward and backward difference formulae. Computation of first and second derivatives.

Numerical integration: General Quadrature formula. Trapezoidal rule, Simpsons $1 / 3^{\text {rd }}$ and $3 / 8^{\text {th }}$ rules, Weddles rule, Problems thereon. Solution of initial value problem for ordinary linear first order differential equations by Picard's, Taylor's, Euler's and Euler's modified method and Fourth Order Runge - Kutta Methods. 45 Hrs

## References:

1. Scheild P: Numerical Analysis (Schaum Series)
2. Sastry S.S.: Numerical Analysis (Prentice Hall of India).
3. Rajaram V.: Computer Oriented Numerical Method (Prentice Hall of India).
4. Balaguruswamy E.: Numerical Methods (Tata McGraw Hill).
5. M.K.Jain, S.R.K. Iyangar and R.K. Jain: Numerical Methods (New Age Int.)
6. G.K.Ranganath: College Mathematics, Vol. III, S. Chand \& Co. Ltd.

## Trigonometry:

Expression of sine and cosines using De-Moiver's theorem. Series of sines and cosines. Hyperbolic functions. Logarithm of a complex number (Simple examples) Summation of trigonometric series (simple problems).

## Complex Analysis:

Recapitulation of Complex numbers, the complex plane, conjugate and modulus of a complex number. The polar form, geometrical representation, Euler's formula $e^{i \theta}=\cos \theta+i \sin \theta$. Functions of complex variables: Limit, continuity and differentiability.

Analytic functions, Cauchy-Reimann equations in Cartesian and polar forms. Sufficient conditions for analyticity (in Cartesian form). Real and imaginary parts of analytic function which are harmonic. Construction of analytic function, given real and imaginary parts.

The complex line integral: Examples and properties (definitions of the concepts like neighborhood of a point, closed contour, etc. at appropriate places should be mentioned).

Cauchy integral theorem (statement) and its consequences. The Cauchy's integral formulae for the function and derivatives. Applications to the evaluation of simple line integrals. Cauchy's inequality. Liouille's theorem-Fundamental theorem of algebra Residue theorem with examples.

## Improper Integrals:

Improper integrals of the first and second kinds. Convergence-Gamma and Beta functions, normal probability integral and error functions, results following the definitions - connection between two functions, applications to evaluation of integrals. Duplication formulae, Sterling formulae (Statements).

## References:

1. Churchill R.V.: Introduction to Complex Variables and Applications (McGraw Hill).
2. Murray R. Spiegel: Complex Variables (Schaum Series).
3. Choudhary B.: The Elements of Complex Analysis (Wiley Eastern).
4. L.V. Ahifors: Complex Analysis (McGraw Hill).
5. Murray R.Spiegel: Advanced Calculus (Schaum Series).
6. Sokoilnikoff I.S.: Advanced Calculus (McGraw Hill).
7. G.K.Ranganath: College Mathematics, Vol. III, S. Chand \& Co. Ltd.

## OPTIONALS

## PAPER 5.3(a): MECHANICS-I

## Dynamics of a Particle and System of Particles:

Conservation principle. Mechanics of particle-conservation of linear momentum, angular momentum and energy. Mechanics and system of particles conservation of linear momentum, angular momentum and energy.

Tangential and normal components of velocity and acceleration. Constrained motion of a particle under gravity along, inside and outside of a circle and a cycloid. Radial and transverse compounds of velocity and acceleration. Motion of a particle in a central force field, determination of orbit from central forces and vice versa, Kepler's law of planetary motion.

## Dynamics of Rigid Bodies:

Centre of mass of a rigid body, static equilibrium of rigid body, rotation of rigid body about a fixed axes. Moment of inertia. Laminar motion of a rigid body, body rolling down an inclined plane. Angular momentum of a rigid body. Product of intertia, moment of intertia of a rigid body, about an arbitrary axes, momental ellipsoid. D'Alembert's principle, General equation of motion of a rigid body, motion of centre of inertia, motion relative to centre of inertia.

## References:

1. S.L.Gupta, V.Kumar and H.V.Sharma: Classical Mechanics, Pragati Prakashan, Meerut.
2. F.Chorlton: Textbook of Dynamics, CBS Publishers, New Delhi.
3. Murray R Spiegel: Theoretical Mechanics, Schaum Series.
4. S.L.Loney: An Elementary treatise on the dynamics of a particle and of rigid bodies, Cambridge University Press, 1958.
5. Grant R.Fowles: Analytical Mechanics, Holt, Rinehart and Winston Inc.

## PAPER 5.3(b): THEORY OF GRAPHS-I

Introduction, graphs, finite and null graphs. Connectedness and component, degree of vertex, minimum and maximum degree, $\Sigma \operatorname{deg} v_{i}=2 v$. The number of vertices of odd degree is even. Isomorphism, complete graph, line graph, total graph.
Sub-graph, spanning and induced sub-graphs, walk, trail, path, cycle, the shortest path problems, bipartite graph. Characterization of bipartite graph in terms of its cycles.

Matrix representation: Incidence, adjacency, rank of a matrix, cyclic matrices, some applications.

## References:

1. Robin J. Wilson: Introduction to Graph Theory, Longman (London), UK.
2. Narsing Deo: Graph Theory \& Applications (PHI), India.
3. Frank Harrary: Graph Theory Narosa Publications, India.

## PAPER 6.3(a): MECHANICS-II

## Analytical Statics:

Resolution of forces in two and three-dimensions, parallelogram law, triangular law of forces, Lamis theorem. Resultant of parallel forces, couples, moment of a couple, Varignan's theorem and theorem of couples.

A system of forces acting in one plane at different points of a body be reduced to a single force through a given point and couple. A static equilibrium, General conditions of equilibrium, common catenary.

## Hydrostatics:

Pressure equation, condition of equilibrium, lines of force, surface of equal pressure, pressure in fluids, centre of pressure, resultant pressure on plane and curved surfaces.

Equilibrium of floating bodies, curves and surfaces of buoyancy, stability of hydrostatic equilibrium of floating bodies, meta centre, work done in producing a displacement, vessel containing liquid.

## References:

1. S.L. Loney:Statics, McMillan \& Co. London.
2. R.S. Verma: A Textbook on Statics, Pothishala Publ. Allahabad.
3. M.Ray and P.T. Chandi: Statics.
4. W.H. Besant \& A.S. Ramsey: A Treatise on Hydromechanics: Part-I Hydrostatics, ELBS \& G Bell \& Sons Ltd., London.

## PAPER 6.3(b): THEORY OF GRAPH-II

Cut vertex, bridge, block, tree, spanning tree, rooted and binary trees, forest. Some properties of trees, characterizations and some examples.

## Connectivity:

Vertex and edge connectivity. Separability, Whitney's inequality $K(G) \leq \lambda(G) \leq \delta(G)$. Menger's theorem statement.

## Eulerian and Hamiltonian Graphs:

Introduction. The Konigsberg Bridge (new name as Kaliningrad) problem and travelling salesmen problem.

Characterization of Eulerian graphs and properties of Hamiltonian graphs. Some applications of graphs in electronic network. 20 hrs

## References:

1. Robin J. Wilson: Introduction to Graph Theory, Longman (London), UK.
2. Narsing Deo: Graph Theory \& Applications (PHI), India.
3. Frank Harrary: Graph Theory, Narosa Publications, India.

# KARNATAKA STATE WOMEN'S UNIVERSITY, BIJAPUR DEPARTMENT OF MATHEMATICS 

Question Paper Pattern for B.Sc. Mathematics Subject
(Semester Scheme)

## SEMESTER-I

## Paper 1.1: Algebra-I:

## Section-A <br> Marks

Answer any Ten of the Following $10 \times 2=20$
1-3 Mathematical Logic
4-6 Elements of Set Theory
7-12 Matrices

## Section-B <br> Marks

Answer any Three of the Following
1-4 Mathematical Logic

## Section-C

Answer any One of the Following
$1 \times 5=5$
1-2 Elements of Set Theory
Section-D Marks
Answer any Four of the Following $\quad 4 \times 5=20$
1-5 Matrices

## Paper 1.2: Calculus-I:

Section-A Marks
Answer any Ten of the Following $\quad 10 \times 2=20$
1-2 Limit \& Continuity
3 Successive Differentiation
4-6 Polar Coordinate
7-12 Theory of Plane Curves

## Section-B

Answer any Four of the Following $4 \times 5=20$
1-2 Up to Successive Differentiation
3-5 Polar Coordinate

## Section-C

Answer any Four of the following
$4 \times 5=20$
1-5 Theory of Plane Curves

## SEMESTER-II

## Paper 2.1: Algebra-II

Section-A:
Answer any Ten of the following $10 \times 2=20$
1-4 Theory of Equation
5-8 Sequences
9-12 Infinite Series

## Section-B:

Answer any Two of the following:
$2 \times 5=10$
1-3 Theory of Equations

## Section-C:

Answer any Three of the following: $3 \times 5=15$
1-4 Sequences
Section-D:
Answer any Three of the following:
$3 \times 5=15$
1-4 Infinite Series
Paper 2.2: Calculus-II:

## Section-A:

Answer any Ten of the following
1-4 Integral Calculus
7-9 Applications of Integral Calculus
10-12 Functions of Two and Three Variables

## Section-B:

Answer any Five of the following:
$5 \times 5=25$
1-3 Integration
4-6 Applications of Integral Calculus.
Section-C:
Answer any Three of the following:
$5 \times 3=15$

## SEMESTER-III

## Paper 3.1: Vectors and Solid Geometry

## Section-A:

$$
\text { Answer any Ten of the following: } \quad 2 \times 10=20
$$

1-3 Vector Algebra
4-12 3-D Geometry

## Section-B:

Answer any Two of the following: $2 \times 5=10$
1-3 Vector Algebra

## Section-C:

Answer any Three of the following: $3 \times 5=15$
1-4 Portion before equation of planes

## Section-D:

Answer any Three of the following:
1-4 Equation of Planes, etc.

## Paper 3.2: Real Analysis:

Section-A:
Answer any Ten of the following: $2 \times 10=20$
1-5 Differentiability
6-8 Riemann Integration
9-12 Line and Multiple Integrals

## Section-B:

Answer any Two of the following:
1-3 Riemann Integration (Portion from upper and lower sums)
Section-C:
Answer any Three of the following:
$5 \times 3=15$
1-4 Differentiability

## Section-D:

Answer any Three of the following:
1-4 Line \& Multiple Integrals

## SEMESTER-IV

## Paper 4.1: Algebra-III

## Section-A:

Answer any Ten of the following: $10 \times 2=20$
1-4 Group Theory
5-7 Rings \& Others
8-12 Linear Algebra

## Section-B:

Answer any Three of the following: $3 \times 5=15$
1-4 Groups

## Section-C:

Answer any Two of the following: $2 \times 5=10$
1-3 Rings \& Others

## Section-D:

Answer any Three of the following: $3 \times 5=15$
1-4 Linear Algebra

## Paper 4.2: Differential Equations-I

## Section-A:

Answer any Ten of the following:
1-4 Ordinary Differential Equations (up to Singular Solution)
5-8 Linear Differential Equation \& Cauchy Euler Equation
9-12 Second Order Linear Differential Equations

## Section-B:

Answer any Three of the following: $3 \times 5=15$
1-4 Up to Singular Solution

## Section-C:

Answer any Three of the following:
1-4 Linear Equations, Cauchy's Euler Equation \& Simultaneous differential equations

## Section-D:

Answer any Two of the following:
1-3 Second Order Linear Differential Equations (One on each method)

## SEMESTER-V

## Paper 5.1: Vector Analysis \& Laplace Transforms:

## Section-A:

Answer any Ten of the following:
1-4 Vector Analysis
5-7 Fourier Series
8-12 Laplace Transformation
Section-B:
Answer any Five of the following: ..... $5 \times 6=30$
1-3 Vector Analysis
4-6 Fourier Series
Section-C:
Answer any Five of the following: ..... $5 \times 6=30$
1-4 Laplace Transformation
5-6 Including applications
Paper 5.2: Differential Equations-II
Section-A:
Answer any Ten of the following: ..... $10 \times 2=20$
1-5 Series Solutions
6-7 Total Differential Equations
8-12 Partial Differential Equations

## Section-B:

Answer any Five of the following:
1-3 Series Solutions
4-6 Total Differential Equations
Section-C:
Answer any Five of the following: ..... $5 \times 6=30$
1-6 Partial Differential Equations

## SEMESTER-VI

## Paper 6.1: Numerical Analysis:

## Section-A:

Answer any Ten of the following: $10 \times 2=20$
1-4 Errors, Solution of Non-Linear Equations \& System of Equations
5-7 Finite Difference, Interpolation, Numerical Differentiation
8-12 Numerical Integration, Solution of IVP.

## Section-B:

Answer any Five of the following:
$5 \times 6=30$
1-3 Errors, Solution of Non-linear Equations, System of Equations
4-6 Finite Differences, Interpolation

## Section-C:

Answer any Five of the following: $\quad 5 \times 6=30$
1-2 Numerical Differentiation
3-4 Numerical Integration
5-6 Solution of IVP

## Paper 6.2: Complex Analysis and Improper Integrals

## Section-A:

Answer any Ten of the following:
1-4 Trigonometry
5-8 Analytic Function and Complex Line Integrals
9-12 Improper Integrals

## Section-B:

Answer any Five of the following:
$5 \times 6=30$
1-6 Analytic Functions, Complex Line Integrals

## Section-C:

Answer any Five of the following:
1-2 Trigonometry
3-6 Improper Integrals

Note: Similar Pattern of Question Papers should be set for the Papers 5.3(a), 5.3(b), 6.3(a) and 6.3(b).

